

Summarizing Search Modeling Examples

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Tic Tac Toe – Set based Search Modeling

$$R = \{1, \dots, 3\}$$

$$M = \{X, O, B\}$$

$$F = \{ (i, j, m) \mid \forall i, j \in R, \forall m \in M \}$$

$$S = \{ F' \subseteq F \mid \text{Covered}(F') \wedge \text{AllUnique}(F') \wedge \text{PlayOrderPreserved}(F') \}$$

$$\text{Covered}(F) \leftrightarrow \forall i, j \in R \exists m \in M \mid (i, j, m) \in F$$

$$\text{AllUnique}(F) \leftrightarrow \forall i, j \in R \forall m, m' \in M \mid ((i, j, m) \in F \wedge (i, j, m') \in F) \rightarrow (m = m')$$

$$\text{PlayOrderPreserved}(F) \leftrightarrow 0 \leq (\text{Count}(X, F) - \text{Count}(O, F)) \leq 1$$

$$\text{Count}(m, F) = \mid \{ (i, j, m) \in F, \forall i, j \in R \} \mid$$

0-1 Knapsack Problem – Set based Search Modeling

$$\text{Weights } W = \langle w_1, \dots, w_n \rangle$$

$$\text{Values } V = \langle v_1, \dots, v_n \rangle$$

$$F = \{ 1, \dots, n \}$$

$$S = \{ F' \subseteq F \mid \sum_{f \in F'} w_f \leq C \}$$

$$\text{Ext} = \{ A \rightarrow B \mid \forall s \in S \bullet A \subseteq s \mid ((s-A) \cup B) \in S \}$$

0-1 Knapsack Problem (GA) – Set based Search Modeling

$$I = \langle (w_1, v_1), \dots, (w_n, v_n) \rangle, C = \text{capacity}$$

$$\text{where } w((w_i, v_i)) = w_i \text{ and } v((w_i, v_i)) = v_i$$

$$F = \{ \{ i_1, \dots, i_m \} \mid (\sum_{j=1..m} w(i_j) \leq C) \}$$

$$S = \{ F' \subseteq 2^F \mid \sum_{f \in F'} w_f \leq C \}$$

$$\text{Ext} = \{ A \rightarrow B \mid \forall s \in S \bullet A \subseteq s \mid (s-A) \cup B \in S \wedge (\text{Mutation}(A, B) \vee \text{Combination}(A, B)) \}$$

$$\text{Mutation}(A, B) \leftrightarrow A = \{ P \} \wedge B = \{ (P - K) \cup J \}$$

$$\text{where } K \subseteq P, J \subseteq I \text{ and } (K \cap J) = \emptyset$$

$$\text{Combination}(A, B) \leftrightarrow A = \{ P, Q \} \wedge B = \{ K \}$$

where $K \subseteq (P \cup Q) \wedge (K \neq P) \wedge (K \neq Q) \wedge \min(|P|, |Q|) \leq |K| \leq \max(|P|, |Q|)$

Model Elimination Problem - And-Tree Search Modeling

C – the set of all clauses (our formal language)

$\text{Prob}_{\wedge, \text{me}} \subseteq 2^C$ (me stands for model elimination)

Solution Definition

$\text{Erw}_{\wedge, \text{me}}((pr, ?), (pr, \text{yes}))$

if $P, \neg P' \in pr$, where $\sigma = \text{mgu}(P, P')$

Branching Definition

$\text{Erw}_{\wedge, \text{me}}((pr \cup \{L_1 \vee \dots \vee L_n\}, ?),$

$(pr \cup \{L_1 \vee \dots \vee L_n\}, ?), (pr \cup \{L_1 \vee \dots \vee L_n, L_1\}), \dots, (pr \cup \{L_1 \vee \dots \vee L_n, L_n\}))$

if for some i , $\text{Erw}_{\wedge, \text{me}}((pr \cup \{L_1 \vee \dots \vee L_n, L_i\}, ?), (pr \cup \{L_1 \vee \dots \vee L_n, L_i\}, \text{yes}))$

Workers and Tasks Problem – Or-Tree Search Modeling

Let T be a set of tasks, and W a set of workers

Let $e: T \times W \rightarrow [0, 1]$ be a function mapping tasks and workers onto efficiency ratings.

For a given sequence of tasks $S = \langle t_1, \dots, t_n \rangle$, assign tasks to workers such that:

- the overall time to complete the sequence is minimized, and
- no worker is assigned to a task for which he has an efficiency rating of 0

$pr = \langle S = \langle t_1, \dots, t_n \rangle, A = \langle (w_i, \langle t'_{1i}, \dots, t'_{mi} \rangle) \mid w_i \in W, t'_{ij} \in T \rangle \rangle$

$f(pr) = \min(\{ \sum_{i=1..m_j} (e(t_{ij}, w_j)^{-1}) \mid (w_j, \langle t_{1j}, \dots, t_{mj} \rangle) \in A \})$

$\text{Erw}_{\vee, \text{wt}}((pr, ?), (pr, \text{no})) \leftrightarrow \exists (w_i, \langle t_{1i}, \dots, t_{mi} \rangle) \in A, \exists j \in \{1 \dots m_i\} \mid e(t_{ji}, w_i) = 0$

$\text{Erw}_{\vee, \text{wt}}((pr, ?), (pr, \text{yes})) \leftrightarrow \neg \text{Erw}_{\vee, \text{wt}}((pr, ?), (pr, \text{no}))$ and $|S| = 0$

* where $pr = \langle S, A \rangle$

$\text{Altern}(pr_0, pr_1, \dots, pr_n) \leftrightarrow pr_0 = \langle S, A \rangle, pr_i = \langle S - s_0, \text{Assign}(A, w_i, s_0) \rangle \forall w_i \in W, \forall s_0 \in S$

$\text{Assign}(A, w, s) = A' \text{ s.t. : if } (w, \langle t_1, \dots, t_n \rangle) \in A \text{ then } (w, \langle t_1, \dots, t_n, s \rangle) \in A'$

else $(w, \langle s \rangle) \in A'$